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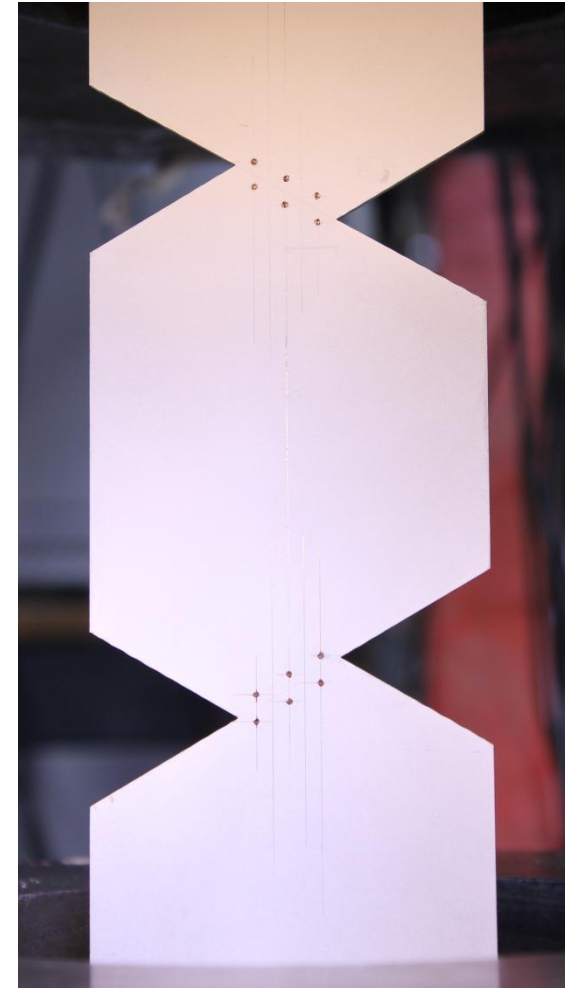
## Notched strip tensile tests to determine the yield characteristics of stainless steel

Jurgen Becque

Maurizio Guadagnini

Ajibola Oyawoye

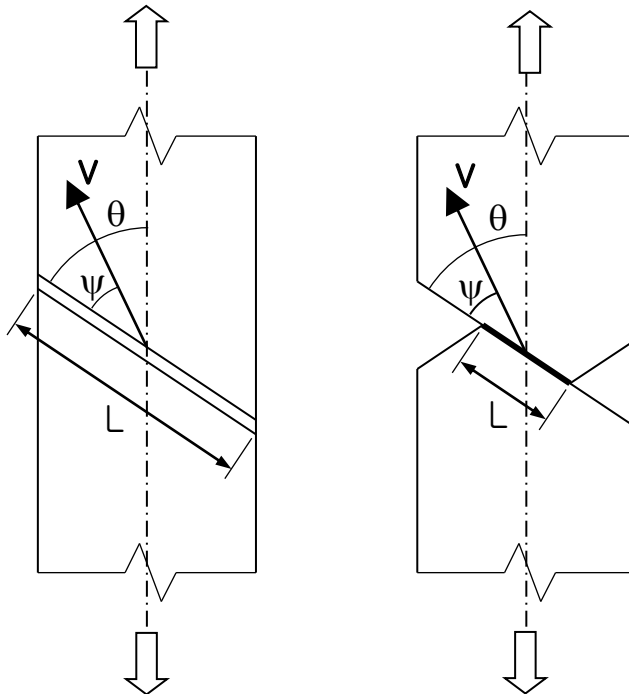
Shan-Shan Huang



# Background

How to subject a material to tension + shear ?

- ➔ tube under internal pressure + torsion
- ➔ tube under axial load + torsion
- ➔ grooved or notched strips (Bijlaard 1940; Hill 1953)



$$55^\circ \leq \theta \leq 90^\circ$$

# Theory

- ⇒ rigid-plastic material
- ⇒ isotropic material
- ⇒ uniform state of stress and strain in the neck

$$\frac{\dot{\varepsilon}_1}{1 + \sin \psi} = \frac{\dot{\varepsilon}_2}{\sin \psi - 1} = \frac{\dot{\varepsilon}_3}{-2 \sin \psi}$$

$$\frac{\sigma_1}{\sin(\theta - \psi) + \cos \theta} = \frac{\sigma_2}{\sin(\theta - \psi) - \cos \theta} = \frac{P}{tL \cos \psi}$$



Lode's parameters

$$\mu = -\frac{\sigma_1 + \sigma_2}{\sigma_1 - \sigma_2} = -\frac{3 \cos \theta - \sin(\theta - \psi)}{\cos \theta + \sin(\theta - \psi)}$$

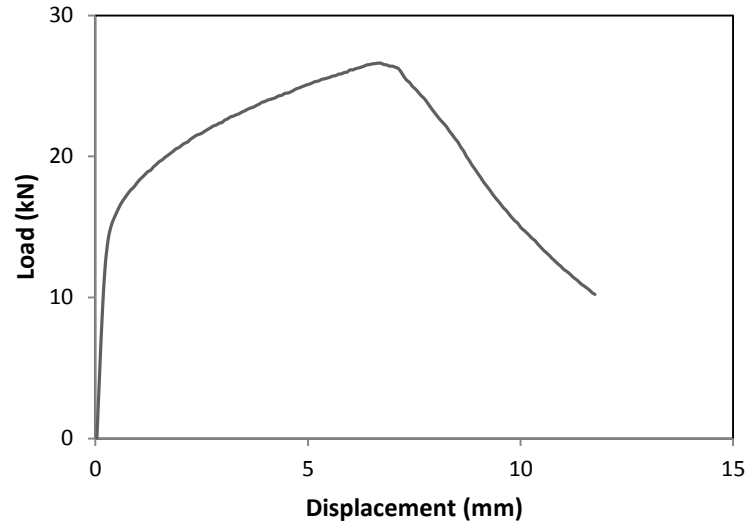
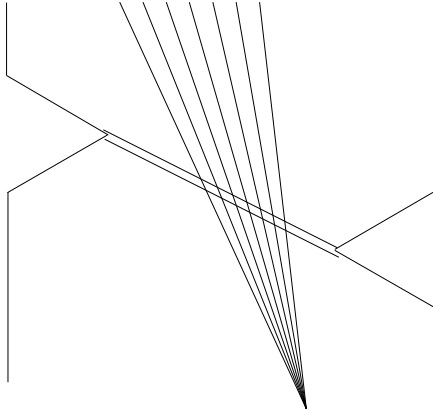
$$\nu = \frac{2\dot{\varepsilon}_2 - \dot{\varepsilon}_1 - \dot{\varepsilon}_3}{\dot{\varepsilon}_1 - \dot{\varepsilon}_3} = -\frac{3(1 - \sin \psi)}{1 + 3 \sin \psi}$$

$$\mu = \nu$$

for the Von Mises  
yield surface

# Problems

- 1 an accurate determination of  $\psi$  is difficult



- 2 an accurate determination of the yield load  $P$  is difficult
- 3 brittle fracture originating from the roots of the notches
- 4 risk of diffuse necking in strain hardening materials
- 5 theory only applies to isotropic materials

# Proposed solutions

## 1 Digital Image Correlation (DIC)

3 } material related (austenitic vs. ferritic)  
4 }  
⇒ sufficiently deep notches

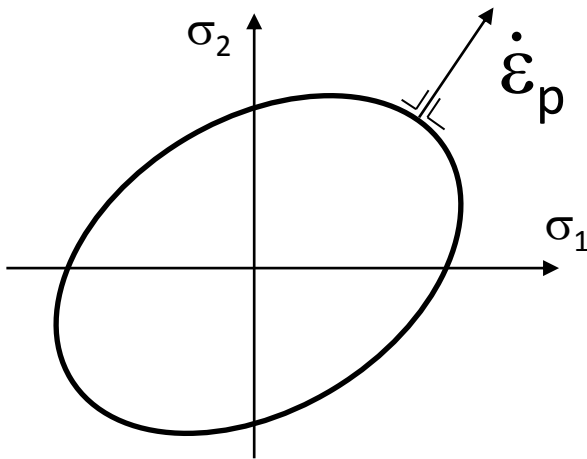
⇒ laser-cut specimens

2 } new theoretical developments needed

5 }  
⇒ anisotropic material  
⇒ eliminate the need to measure  $P$

# New theory

$$F\sigma_y^2 + G\sigma_x^2 + H(\sigma_x - \sigma_y)^2 + 2N\tau_{xy}^2 = \sigma_0^2 \quad (\text{Hill})$$



$(\theta, \psi)$

$$A = \frac{\sin \psi}{\sin(2\theta - \psi)}$$

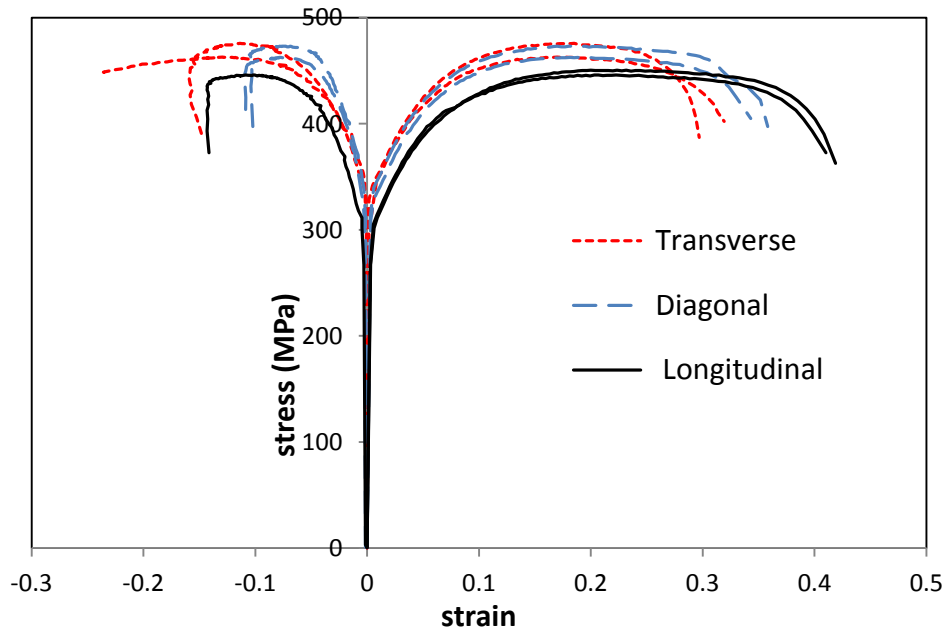
$$B = \frac{2 \sin \psi}{\cos(2\theta - \psi)}$$

$$\frac{F \cos^2 \theta + G \sin^2 \theta + NB \sin \theta \cos \theta}{F(1 + 2 \cos^2 \theta) - G \cos(2\theta) - NB \cos(2\theta) / \tan \theta} = \frac{F(A-1)\cos^2 \theta - G(A+1)\sin^2 \theta + 2HA \cos(2\theta)}{F(A-1)(1 + 2 \cos^2 \theta) + G(A+1)\cos(2\theta) + 8HA \cos^2 \theta}$$

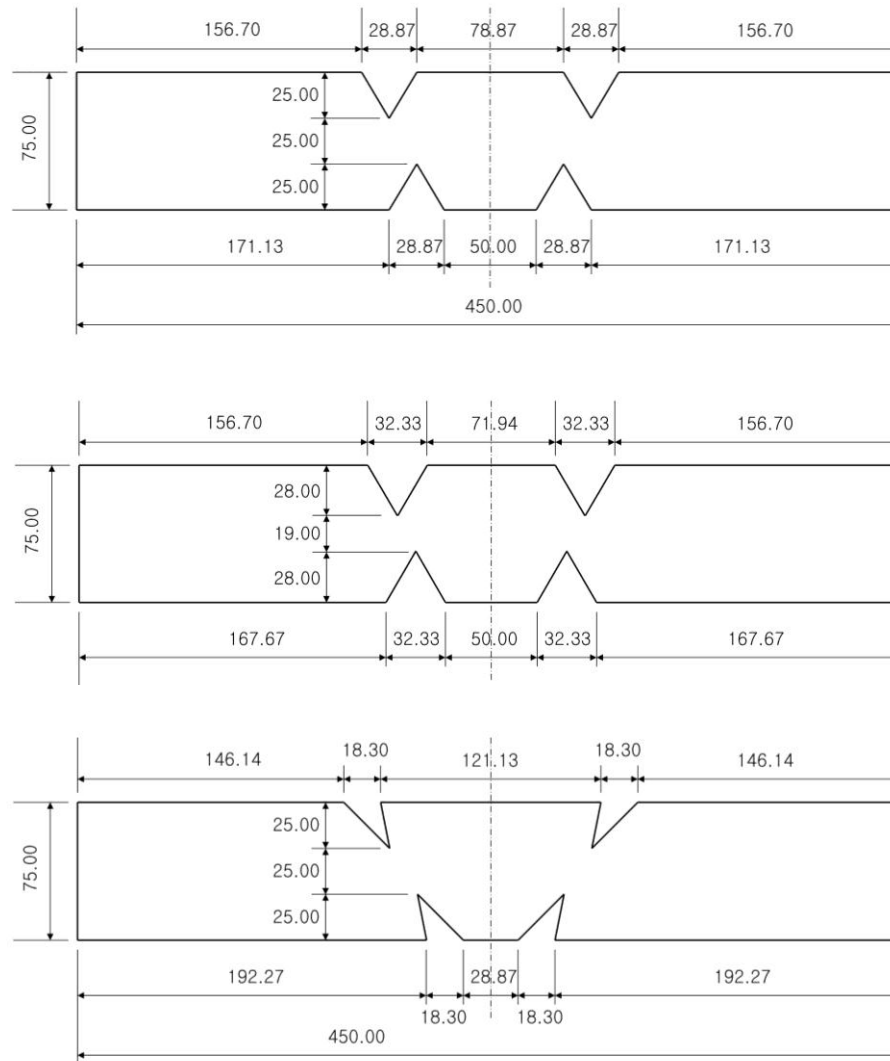
# Experimental program: tensile tests



	430 (1.4016)	304L (1.4301)
Rolling dir.	315 MPa	290 MPa
Diagonal dir.	340 MPa	292 MPa
Transverse dir.	345 MPa	290 MPa



# Experimental program: notched strip tests



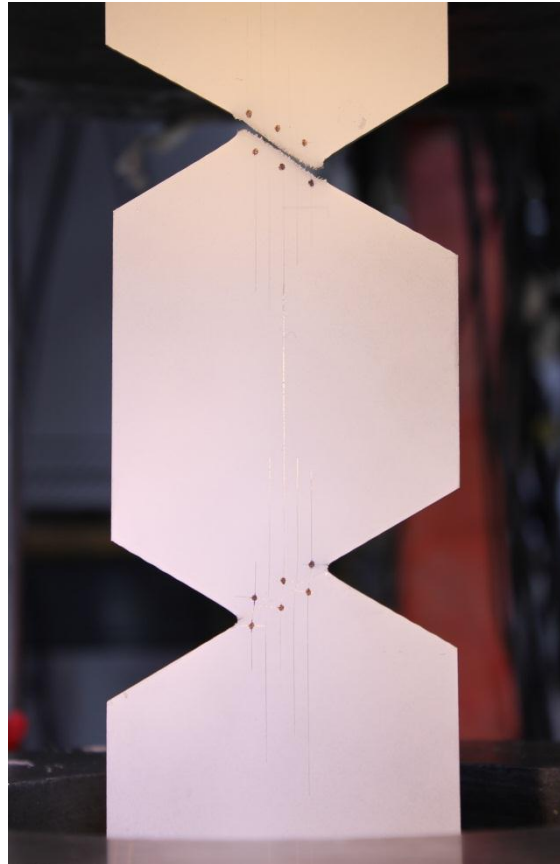
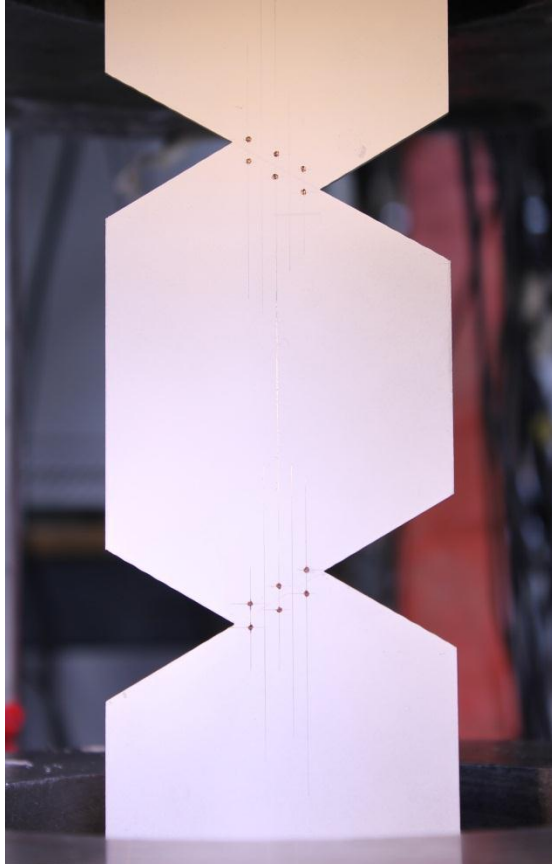
$\theta = 60^\circ$

$\theta = 70^\circ$

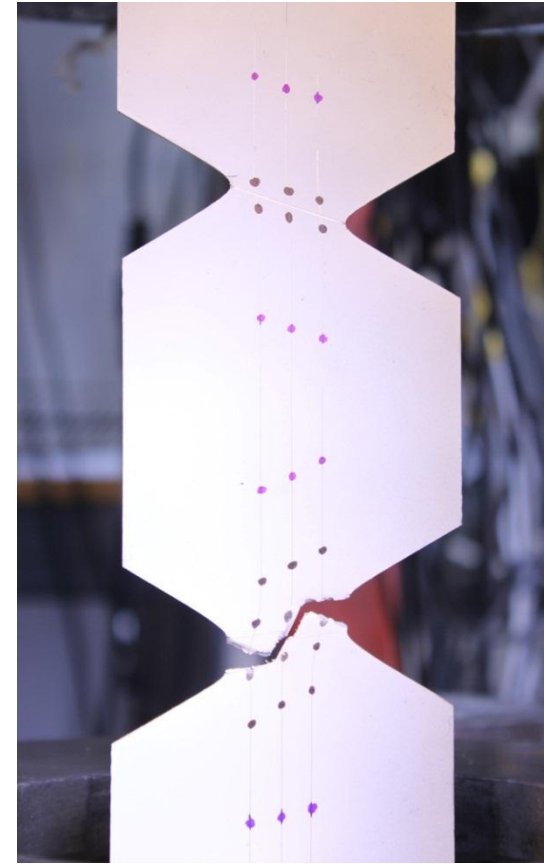
$\theta = 80^\circ$



# Experimental program: notched strip tests

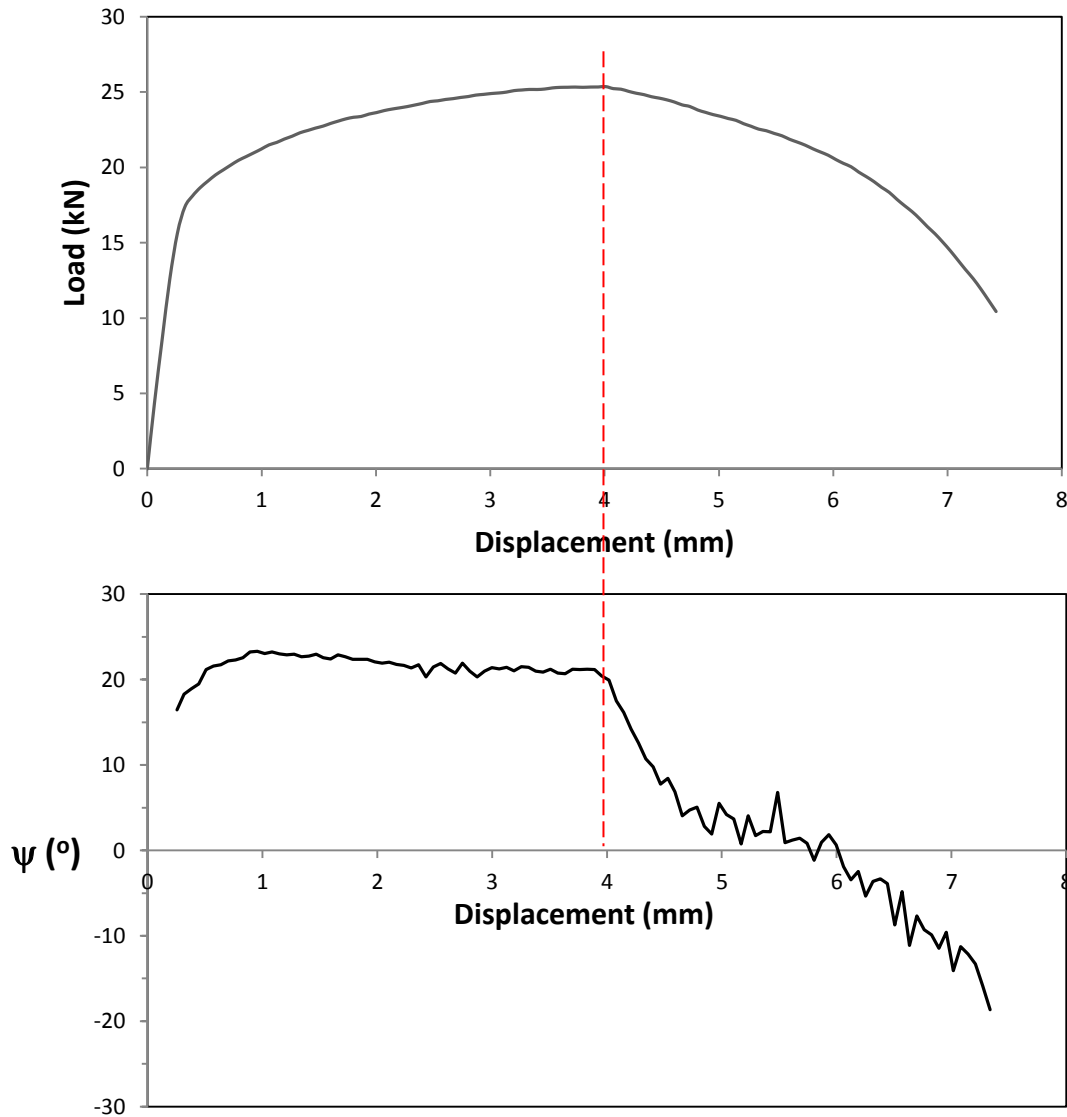


Ferritic



Austenitic

# Results



# Results: 304L austenitic

Specimen	$\theta$	$\psi$	$\psi$ (theory)	F	G	H	N
	°	°	°	-	-	-	-
NA-0-60-B	60.31	22.21	23.68	0.464	0.464	0.536	1.508
NA-0-70-B	69.86	36.22	34.29	0.534	0.534	0.466	1.438
NA-0-80-B	79.99	56.68	54.77	0.533	0.533	0.467	1.440
NA-90-60-B	59.55	26.84	23.04	0.594	0.594	0.406	1.378
NA-90-70-B	69.63	33.58	33.95	0.490	0.490	0.510	1.483
NA-90-80-B	80.12	55.84	55.13	0.509	0.509	0.491	1.464
Average				0.521	0.521	0.479	1.452
COV				0.086	0.086	0.093	0.031

Average difference = 1.08°

# Results: 430 ferritic

Specimen	$\theta$	$\psi$	$\psi$ (theory)	F	G	H	N
	°	°	°	-	-	-	-
NF-0-60-B	60.17	26.43	23.56	0.573	0.411	0.427	1.232
NF-0-70-B	69.90	37.97	34.34	0.582	0.420	0.418	1.224
NF-0-80-B	80.30	57.50	55.63	0.555	0.393	0.445	1.251
NF-90-60-B	60.62	21.06	23.95	0.504	0.342	0.496	1.302
NF-90-70-B	70.04	31.74	34.55	0.497	0.335	0.503	1.308
NF-90-80-B	79.81	58.23	54.28	0.602	0.440	0.398	1.204
NF-0-60-D	60.36	22.72	23.72	0.480	0.318	0.520	1.326
NF-0-70-D	69.85	36.91	34.27	0.563	0.401	0.437	1.243
NF-0-80-D	80.41	54.72	55.94	0.501	0.339	0.499	1.304
NF-0-60-S	59.70	25.96	23.17	0.572	0.410	0.428	1.234
NF-0-70-S	69.92	39.75	34.37	0.616	0.454	0.384	1.189
NF-0-80-S	79.66	60.44	53.87	0.653	0.491	0.347	1.153

Average <sup>1</sup>	0.540	0.378	0.460	1.266
COV <sup>1</sup>	0.082	0.117	0.096	0.035

# Conclusions

Notched strip tests have the potential to provide an easy-to-use method to determine the yield surface of stainless steel alloys, provided that:

- ⇒ DIC is used as a measurement method
- ⇒ the method is used in conjunction with new theoretical developments which account for anisotropy and eliminate the need for measurements of the applied load